

# Cambridge International AS & A Level

---

**MATHEMATICS****9709/12**

Paper 1 Pure Mathematics 1

**October/November 2025**

MARK SCHEME

Maximum Mark: 75

---

**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

---

This document consists of **25** printed pages.

**PUBLISHED****Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**PUBLISHED****Mathematics-Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

Kambridge Math & Physics  
kambridgemp.com










**PUBLISHED****Annotations guidance for centres**

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.


We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.





**Annotations**

<b>Annotation</b>	<b>Meaning</b>
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect
Dep	Used to indicate DM0 or DM1

**PUBLISHED**

<b>Annotation</b>	<b>Meaning</b>
DM1	Dependent on the previous M1 mark(s)
<b>FT</b>	Follow through
	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
<b>ISW</b>	Ignore subsequent work
<b>J</b>	Judgement
<b>JU</b>	Judgement
<b>M0</b>	Method mark awarded zero
<b>M1</b>	Method mark awarded one
<b>M2</b>	Method mark awarded two
<b>MR</b>	Misread
<b>O</b>	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
<b>PE</b>	Judgment made by the PE
<b>Pre</b>	Premature approximation
<b>SC</b>	Special case
<b>SEEN</b>	Indicates that work/page has been seen

**PUBLISHED**

Annotation	Meaning
	Error in number of significant figures
	Correct
	Transcription error
	Correct answer from incorrect working

Kambridge Math & Physics  
kambridgemp.com

**PUBLISHED****Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

**Types of mark**

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
  - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
  - The total number of marks available for each question is shown at the bottom of the Marks column.
  - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
  - Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

**Abbreviations**

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

Kambridge Math & Physics  
kambridgemp.com

## PUBLISHED

Question	Answer	Marks	Guidance
1(a)	$\{9\} \{(x-2)^2\} \{-28\}$	<b>B2,1,0</b>	B2 for all 3 correct values. B1 for any two correct. Allow $p=9, q=-2, r=-28$ . If contradictory, give preference to the expression. Condone correct values in an expression of the correct form, even if missing the square on the bracket. Allow B1 for $9\{(x-2)^2+k\}$ .
		<b>2</b>	
1(b)	$k < -28$	<b>B1FT</b>	$k < \text{their } r$ .
		<b>1</b>	
1(c)	$9(x - \text{their } 2)^2 - \text{their } 28 = -15 \Rightarrow (x-2)^2 = \frac{13}{9}$ or $x = \frac{36 \pm \sqrt{36^2 - 4 \times 9 \times 23}}{2 \times 9}$	<b>M1</b>	Solving as far as ' $(x+q)^2 =$ '. Allow sign errors only in the rearrangement, or rearranging and using the quadratic formula (see quadratics guidance).
		<b>A1</b>	ISW if decimals given after the exact answers.
		<b>2</b>	
	$x = 2 \pm \frac{\sqrt{13}}{3}$ or $\frac{6 \pm \sqrt{13}}{3}$ or $2 \pm \sqrt{\frac{13}{9}}$ or $\frac{36 \pm \sqrt{468}}{18}$ oe		

**PUBLISHED**

Question	Answer	Marks	Guidance
2	$\binom{6}{2} \times (2x^2)^2 \times \left(-\frac{3}{x}\right)^{6-2}$ or $\binom{6}{2} \times 2^6 \times (x^2)^2 \times \left(-\frac{3}{2x}\right)^{6-2}$	<b>B1</b>	$\binom{6}{2}$ may be replaced by $\binom{6}{4}$ or 15. May be seen in a list. Condone missing brackets only if recovered later.
	Identifying the relevant term of the form: $k \times (2x^2)^2 \times \left(-\frac{3}{x}\right)^{6-2}$ or $k \times 2^6 \times (x^2)^2 \times \left(-\frac{3}{2x}\right)^{6-2}$	<b>M1</b>	May still be part of a list if, e.g., underlining or arrow. $k$ can be any constant or any $\binom{p}{q}$ . May be implied by correct final answer. If constants evaluated, then condone errors for this mark.
	= 4860	<b>A1</b>	Accept $4860x^0$ <b>SC B2</b> for $-4860$
		<b>3</b>	

**PUBLISHED**

Question	Answer	Marks	Guidance
3(a)	Translation $\begin{pmatrix} 0 \\ 2 \end{pmatrix}$ , or Translation 2 ‘parallel to the $y$ -axis’ or ‘in the $y$ -direction’ or ‘vertically’.	<b>B1</b>	Condone ‘shift’ and vector written as co-ordinates. Allow any mention of the $y$ -axis but not just ‘up’.
	{Stretch} {factor $\frac{1}{3}$ } {parallel to $x$ -axis or in $x$ -direction or horizontally}	<b>B2,1,0</b>	B2 for 3 correct components. B1 for 2. Allow ‘the $y$ -axis is invariant’.
		<b>3</b>	
3(b)	$[y = ]3g(-x)$	<b>B2,1,0</b>	B1 for 3 outside the function and nowhere else, or – inside the function and nowhere else. So $-3g(x)$ , $3(-gx)$ , $g(-3x)$ , $g\left(\frac{x}{-3}\right)$ , $3g(x) + 2$ , $-3g(-x)$ and $3g(-3x)$ all score B1. But $3g(3x)$ , $-g(-x)$ score B0. <b>SC B1</b> for $3f(-x)$ .
		<b>2</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
4(a)	$[k =]4$	<b>B1</b>	
		<b>1</b>	
4(b)	$\left\{ \frac{k}{4}x^4 \right\} + \left\{ \frac{2x^{-2+1}}{-2+1} \right\} [+c]$	<b>B2,1,0FT</b>	FT <i>their k</i> from <b>4(a)</b> or the letter <i>k</i> . B2 for both correct components and no other <i>x</i> -terms. B1 for one correct.
	$20 = \frac{\textit{their k}}{4} \times 2^4 - \frac{2}{2} + c$	<b>M1</b>	Substituting $x = 2$ and $y = 20$ into <i>their</i> integrated expression (defined by having at least one correct power and including a '+ c'). Allow one slip.
	$c = 5$	<b>A1</b>	
	$[t =]4$	<b>A1</b>	
			<b>5</b>

## PUBLISHED

Question	Answer	Marks	Guidance
5(a)	$\left[\frac{dy}{dx} = \right] 2x^{-\frac{1}{2}} - 1$	<b>B1</b>	
	$2x^{-\frac{1}{2}} - 1 = 0 \Rightarrow x^{\frac{1}{2}} = 2$	<b>M1</b>	Setting <i>their</i> $\frac{dy}{dx}$ of the form $kx^{-\frac{1}{2}} - 1$ equal to 0 and solving as far as $x^{\frac{1}{2}} = d$ , condoning sign errors only. Can be implied by correct final answer but not if clearly following wrong working.
	$[a = ]4$	<b>A1</b>	
<b>Alternative Method for Question 5(a):</b>			
	$y = 4\sqrt{x} - (\sqrt{x})^2$	<b>B1</b>	Recognising the quadratic in $\sqrt{x}$ .
	Max at $\sqrt{x} = \frac{-b}{2a} = \frac{-4}{-2} = 2$ or $-(\sqrt{x} - 2)^2 + 4 \Rightarrow x^{\frac{1}{2}} = 2$	<b>M1</b>	Condone sign errors only. Allow $z = \sqrt{x}$ , $-(z - 2)^2 + 4 \Rightarrow \text{max at } 2$ .
	$[a = ]4$	<b>A1</b>	
		<b>3</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
5(b)	$[x = \text{or } b =] 16$	<b>B1</b>	SOI It may be found in <b>5(a)</b> , but must be seen in <b>5(b)</b> . Condone extra ‘solution’ $x = 0$ .
	$\left[ \int (4x^{\frac{1}{2}} - x) dx = \right] \left\{ \frac{4}{\frac{3}{2}} x^{\frac{3}{2}} \right\} + \left\{ -\frac{1}{2} x^2 \right\}$	<b>B2, 1, 0</b>	B2 for both correct components and no other $x$ terms. B1 for one correct term. Allow any correct unsimplified form.
	$[\text{Area} =] \left( \frac{8}{3} \times 16^{\frac{3}{2}} - \frac{1}{2} \times 16^2 \right) - \left( \frac{8}{3} \times 4^{\frac{3}{2}} - \frac{1}{2} \times 4^2 \right)$	<b>M1</b>	Substituting <i>their a</i> (from part <b>(a)</b> ) and <i>their b</i> (from an attempt to solve $4x^{\frac{1}{2}} - x = 0$ ) into an integrated expression (defined by having at least one correct power) and subtracting. If correct limits and integration, then minimum acceptable working is $\frac{128}{3} - \frac{40}{3}$ . If incorrect limits or integration, then full substitution of every term must be seen. Note: needs $0 < a < b$ , otherwise M0, but allow limits applied either way round. Allow missing brackets if recovered.
	$\left\{ = \frac{128}{3} - \frac{40}{3} \right\} = \frac{88}{3} \text{ or } 29\frac{1}{3}$	<b>DB1</b>	Must be exact. Allow $-\frac{88}{3}$ if it becomes $\frac{88}{3}$ . Do not ISW if a further area is added or subtracted. Dependent upon B1B2 scored earlier.
		<b>5</b>	

**PUBLISHED**

Question	Answer	Marks	Guidance
6(a)		<b>B2, 1, 0</b>	<p>B2 Fully correct curve, including 2, 5 and <math>-1</math> clearly labelled or implied on the <math>y</math>-axis and the curve horizontal only at <math>(\frac{1}{2}\pi, 5)</math> and <math>(\frac{3}{2}\pi, -1)</math> (approximately).                      Condone the <math>x</math>-axis intercepts and the stationary points not being in exactly the correct positions and <math>y</math>-axis not to scale.                      B1 for one full cycle from 0 to <math>2\pi</math> starting on the positive <math>y</math>-axis and initially increasing.                      Note: Starting at the origin or finishing at <math>(2\pi, 0)</math> scores B0.</p>
		2	
6(b)(i)	1	<b>B1</b>	Ignore any working out seen or graphs drawn.
		1	
6(b)(ii)	3	<b>B1</b>	
		1	

## PUBLISHED

Question	Answer	Marks	Guidance
6(c)	$3\sin x + 2 = 5(1 - \sin^2 x) - 1$	<b>M1*</b>	For replacing $\cos^2 x$ with $1 - \sin^2 x$ .
	$5\sin^2 x + 3\sin x - 2 \quad [=0]$	<b>DM1</b>	For simplifying to a 3-term quadratic. The terms don't all need to be on the same side. Condone sign errors only. Candidates who miss out the '-1' can score the M1DM1 only.
	$\sin x = 0.4$ and $-1$	<b>A1</b>	
	$x = 0.41, 2.73, \frac{3}{2}\pi$ AWR or $0.13\pi, 0.87\pi, 1.5\pi$ or $\frac{59}{450}\pi, \frac{391}{450}\pi, \frac{3}{2}\pi$	<b>A2, 1, 0</b>	A2 for three correct values and no others in the range $0 \leq x \leq 2\pi$ . A1 for 2 correct values. Ignore $^\circ$ symbol if seen with answers. Ignore answers outside the domain. Allow 4.71 or equivalent fractions instead of $\frac{3}{2}\pi$ <b>SC A1</b> for $23.6^\circ, 156.4^\circ$ AWR and $270^\circ$ or $\frac{3}{2}\pi$ only. <b>SC A1</b> for 0.4, 2.7 and 4.7 or $\frac{3}{2}\pi$ only.
	<b>5</b>		

## PUBLISHED

Question	Answer	Marks	Guidance
7(a)	[Centre is] (4, 6)	<b>B1</b>	SOI
	$\sqrt{3^2 + 5^2}$ or $3^2 + 5^2$ or $\sqrt{6^2 + 10^2}$ or $6^2 + 10^2$ oe	<b>B1</b>	SOI Finding $PQ$ or $PQ^2$ or $\frac{1}{2}PQ$ or $(\frac{1}{2}PQ)^2$ . Allow 5.83 or $5.83^2$ or 11.7 or $11.7^2$ AWRT. Allow unsimplified, e.g. $\sqrt{(4-1)^2 + (6-1)^2}$ .
	$(x - \text{their } 4)^2 + (y - \text{their } 6)^2 = (\text{their radius})^2$	<b>M1</b>	Using what they think that the centre and radius are, correctly, in the equation of a circle. Do not allow $P$ or $Q$ as the centre or the diameter being used as the radius.
	$(x - 4)^2 + (y - 6)^2 = 34$ or $x^2 + y^2 - 8x - 12y + 18 = 0$	<b>A1</b>	May be done by other equivalent method. Do not allow $(\sqrt{34})^2$ or $5.83^2$ for the final answer.
		<b>4</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
7(b)	[Gradient of $PQ$ =] $\frac{11-1}{7-1}$ or $\frac{5}{3}$ oe	<b>B1</b>	Allow unsimplified.
	[Gradient of tangent =] $-\frac{3}{5}$	<b>M1</b>	Use of $m_1m_2 = -1$ with <i>their</i> gradient $PQ$ .
	$\frac{y-11}{x-7} = -\frac{3}{5}$ oe e.g. $y = -\frac{3}{5}x + \frac{76}{5}$	<b>A1</b>	ISW Condone stopping at $c = \frac{76}{5}$ if $y = -\frac{3}{5}x + c$ stated earlier.
	<b>Alternative Method for Question 7(b):</b>		
	$2(x-4) + 2(y-6)\frac{dy}{dx} = 0$	<b>B1</b>	Or rearranging to form ' $y =$ ' and differentiating using the chain rule.
	Substitute $x = 7, y = 11 \Rightarrow 6 + 10\frac{dy}{dx} = 0 \Rightarrow \frac{dy}{dx} = -\frac{3}{5}$	<b>M1</b>	Substituting $x = 7$ and $y = 11$ into a correct differential equation and rearranging to give $\frac{dy}{dx}$ allowing sign errors only.
$\frac{y-11}{x-7} = -\frac{3}{5}$ oe e.g. $y = -\frac{3}{5}x + \frac{76}{5}$	<b>A1</b>		
		<b>3</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
7(c)	y-coordinate of $R$ is 1	<b>B1</b>	
	[Equation of tangent at $R$ is] $\frac{y-1}{x-7} = \frac{3}{5}$ oe eg $y = \frac{3}{5}x - \frac{16}{5}$	<b>B1</b>	
	$\frac{3}{5}(x-7)+1 = -\frac{3}{5}(x-7)+11 \Rightarrow x = \dots$ or $y = \dots$	<b>M1</b>	Using <i>their</i> stated line and the equation from part (b) to reach a value of $x$ or $y$ . Do not allow if the gradients are the same.
	$x = \frac{46}{3}$ oe and $y = 6$	<b>A1</b>	
	<b>Alternate Method for Question 7(c):</b>		
	y-coordinate of $R$ is 1	<b>B1</b>	Can be implied by correct $y$ -coordinate of point of intersection.
	y-coordinate of point of intersection is 6	<b>B1</b>	
	<b>Then either</b>		
	$6-11 = -\frac{3}{5}(x-7)$	<b>M1</b>	Using $y = 6$ in <i>their</i> equation of tangent at $R$ .
	<b>Or</b>		
$(x-4)^2 = 34 + (x-7)^2 + 25$	<b>(M1)</b>	Using the right-angled triangle formed by the centre, $Q$ and the point of intersection of the tangents.	
$x = \frac{46}{3}$ $\left[ \frac{46}{3}, 6 \right]$ oe	<b>A1</b>	Allow 15.3 AWRT.	
	<b>4</b>		

## PUBLISHED

Question	Answer	Marks	Guidance
8(a)	$-3c - b = b - a$ or $2b = a - 3c$ or $\frac{b}{a} = \frac{c}{b}$ or $b^2 = ac$ oe	<b>B1</b>	For one correct equation connecting $a$ , $b$ and $c$ only. Allow $a + 2(b - a) = -3c$ .
	$4ac = (a - 3c)^2$ or $2\sqrt{ac} = a - 3c$ oe	<b>M1</b>	Forming an equation in $a$ and $c$ only using both the AP and GP. Condone sign errors only.
	$\Rightarrow a^2 - 6ac + 9c^2 = 4ac \Rightarrow a^2 - 10ac + 9c^2 = 0$	<b>A1</b>	AG Convincing proof needed, e.g. $(a - 3c)^2$ expanded.
		<b>3</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
8(b)(i)	$81 - 90c + 9c^2 = 0 \Rightarrow [9](c-9)(c-1) = 0$ or $\frac{90 \pm \sqrt{5184}}{18} \left[ = \frac{90 \pm 72}{18} \right]$	<b>M1</b>	Factorising or other accepted method for solving. See quadratics guidance but condone missing the factor 9. Allow presence of $a$ .
	$c = 1$	<b>B1</b>	Condone extra 'solution' $c = 9$ . B0 if any error seen leading to $c = 1$ but all further marks are still available in this part and <b>(b)(ii)</b> .
	$r^2 = \frac{\text{their } 1}{9} \Rightarrow r = \left[ \frac{1}{3} \right],$ or $b^2 = \text{their } 1 \times 9 \Rightarrow b = 3 \Rightarrow r = \left[ \frac{1}{3} \right]$	<b>M1*</b>	Correctly finding a value for $r$ from <i>their</i> $c$ . May be implied by $r = \frac{1}{3}$ or $r = \pm \frac{1}{3}$ or $r = -\frac{1}{3}$ .
	$S_\infty = \frac{9}{1 - \frac{1}{3}}$	<b>DM1</b>	Use of correct sum to infinity formula with 9 and <i>their</i> $ r  < 1$ . Ignore any extra working with a negative value of $r$ .
	$S_\infty = \frac{27}{2}$ oe	<b>A1</b>	Do not condone extra 'answer'. This mark is not dependent upon the first M1.
		<b>5</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
8(b)(ii)	$d = -6$	<b>B1</b>	SOI
	$S_{20} = \frac{20}{2}(2 \times 9 + (20 - 1) \times (-6))$	<b>M1</b>	Use of a correct sum formula with $n = 20$ , $a = 9$ and <i>their</i> non-zero $d$ stated in this part (can be implied by quoting the correct formula then substituting). But allow use of $\pm 6$ without stating either the formula or ' $d =$ '.
	$S_{20} = -960$	<b>A1</b>	
		<b>3</b>	

Question	Answer	Marks	Guidance
9(a)	$\frac{4 \times 3 \times (-2)}{(3x - 6)^3} + \frac{1 \times 3 \times (-3)}{(3x - 6)^4}$ or $4 \times 3 \times (-2)(3x - 6)^{-3} + 1 \times 3 \times (-3)(3x - 6)^{-4}$	<b>B1B1B1</b>	B1 for the correct powers, B1 for $\times 3$ in at least one term, B1 for all correct which can be unsimplified.
	Decreasing.	<b>B1*</b>	This mark is only available if $f'(x)$ is of the form $(-p)(3x - 6)^{-3} + (-q)(3x - 6)^{-4}$ , where $p$ and $q$ are positive coefficients.
		<b>4</b>	
9(b)	$f^{-1}$ exists because $f$ is a decreasing function Or $f^{-1}$ exists because it is one-to-one, or passes the horizontal line test.	<b>DB1</b>	
		<b>1</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
9(c)	$g(x) > 4a - 3$	<b>B1</b>	Allow 'y >' or 'g >' only. Accept $4a - 3 < y < \infty$ or $(4a - 3, \infty)$ . Condone $(4a - 3, \infty]$ . Accept $g(x) > g(a)$ , but not if they make an error 'simplifying' it.
		<b>1</b>	
9(d)	<b>Either</b> $4a - 3 > 2$ allow with $x$ or $a$ or $\geq$	<b>M1</b>	Do not allow = or $\neq$ , unless they reach a correct inequality later.
	$a > \frac{5}{4}$ or $a \geq \frac{5}{4}$ oe	<b>A1</b>	Accept $\frac{5}{4} < a < \infty$ , $\frac{5}{4} \leq a < \infty$ , $(\frac{5}{4}, \infty)$ or $[\frac{5}{4}, \infty]$ .
	<b>Or</b> $3 \times (4a - 3) - 6 > 0$ allow with $x$ or $a$ or $\geq$	<b>M1</b>	Do not allow = or $\neq$ , unless they reach a correct inequality later.
	$a > \frac{5}{4}$ or $a \geq \frac{5}{4}$ oe	<b>A1</b>	Accept $\frac{5}{4} < a < \infty$ , $\frac{5}{4} \leq a < \infty$ , $(\frac{5}{4}, \infty)$ or $[\frac{5}{4}, \infty]$ .
		<b>2</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
10(a)	$s^2 = r^2 + r^2 - 2r^2 \cos \frac{2\pi}{3}$ <p>or <math>\frac{r}{\sin \frac{\pi}{6}} = \frac{s}{\sin \frac{2\pi}{3}}</math></p> <p>or <math>s = 2r \times \cos \frac{\pi}{6}</math></p> <p>or <math>\left(\frac{r}{2}\right)^2 + \left(\frac{s}{2}\right)^2 = r^2</math></p> <p>or <math>\left(\frac{3r}{2}\right)^2 + \left(\frac{s}{2}\right)^2 = s^2</math> oe</p>	<b>M1</b>	Forming a correct equation. Allow use of degrees.
	$\Rightarrow$ E.g. $s = 2r \times \frac{\sqrt{3}}{2} \Rightarrow s = \sqrt{3}r$	<b>A1</b>	<b>AG</b> Convincing proof required. E.g., for those using trig, the exact value of the trig ratio substituted before the final answer is needed.
		<b>2</b>	

## PUBLISHED

Question	Answer	Marks	Guidance
10(b)	[Angle BAD, BAC or CAD =] $\frac{2\pi}{3}$ or $120^\circ$	<b>B1</b>	SOI, unless clearly associated with the wrong angle. Condone 2.09 for this mark only.
	[Sector BAD =] $\frac{1}{2}r^2 \times \frac{2\pi}{3}$ oe	<b>B1</b>	
	[Sector BCD =] $\frac{1}{2}s^2 \times \frac{\pi}{3}$ oe	<b>B1*</b>	
	$= \frac{3}{6}\pi r^2$ or $\frac{1}{2}\pi r^2$	<b>DB1</b>	Sector BCD simplified in terms of $r$ .
	<b>Either</b> [Area triangle ABD, ABC or ACD =] $\frac{1}{2}r^2 \times \sin \frac{2\pi}{3}$ or $\frac{r}{2} \times \frac{s}{2}$ oe	<b>B1*</b>	May be multiplied by 2 or by 3. Note: $\frac{1}{2}r^2 \times \sin \frac{\pi}{3} = \frac{\sqrt{3}}{4}r^2$ is B0DB0.
	$= \frac{\sqrt{3}}{4}r^2$	<b>DB1</b>	May be multiplied by 2 or by 3.
	<b>Or</b> [Area triangle CBD =] $\frac{1}{2}s^2 \times \sin \frac{\pi}{3}$ or $\frac{3r}{2} \times \frac{s}{2}$ oe	<b>(B1*</b>	Note: $\frac{1}{2}s^2 \times \sin \frac{2\pi}{3} = \frac{3\sqrt{3}}{4}r^2$ is B0DB0.
	$= \frac{3\sqrt{3}}{4}r^2$	<b>DB1)</b>	
$\left(\frac{\sqrt{3}}{2} - \frac{\pi}{6}\right)r^2$ or e.g. $\left(\frac{12\sqrt{3} - 4\pi}{24}\right)r^2$ oe in the required exact form	<b>B1</b>	Fully correct solution. Accept $a = \frac{\sqrt{3}}{2}$ , $b = -\frac{\pi}{6}$ .	
		<b>7</b>	